Asynchronous approach in the plane: A deterministic polynomial algorithm¹

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Deterministically bring two mobile asynchronous agents initially separated within each other's range of vision/communication





















Czyzowicz, Pelc, and Labourel

Deterministic approach algorithm whose cost (total distance traveled) is exponential in D, the initial distance between the agents.

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Tunnels

Two routes r_1 and r_2 respectively from nodes v_1 and v_2 form a *tunnel* iff r_1 has a prefix p which ends at v_2 and r_2 has a prefix which is \overline{p} *i.e.*, the reverse of p.

A first exponential solution



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Bampas, Czyzowicz, Gasieniec, Ilcinkas, and Labourel

The agents know the coordinates of their initial location in a common coordinate system (some kind of GPS). Nearly optimal solution.

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Dieudonné and Pelc

Each agent is assigned a constant speed which cannot change afterwards.

Reduction to rendez-vous in the infinite grid





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Deterministic algorithm whose cost (total number of edge traversals) is polynomial in the initial distance D and the length of the shorter label.

Simplifying assumption

Assume a synchronous setting

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First issue

Initial separating distance D unknown

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Solution: phases

Perform successive tests called phases:

During each test, the agents act as if the tested value were the good one. Phase $i \to$ Tested value 2^i

Phase	Phase	Phase	 Phase	Phase
0	1	2	π-1	π

Phase	Phase	Phase	 Phase	Phase
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The good phase

Phase π with $2^{\pi-1} < D \leq 2^{\pi}$

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Dessmark, Fraigniaud, Kowalski, and Pelc

Roughly speaking: each agent reads a binary sequence obtained from its label until they read different bits.
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The good phase (update)

Phase π with $2^{\pi-1} < max\{D, \lambda\} \le 2^{\pi}$









So far, well known techniques.

From now on, we get into our actual contribution.

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Either they meet or the later agent makes some progress.

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- Second one: between phases, pushes the previous phases

Removing the synchronous setting assumption







Waiting does not work!









Small break (1)



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Let us use reverse routes and tunnels.






























Let us make v_0 the first node from which A_1 follows R_0 during its R_1 . Once again, we use tests separated by the first synchronization mechanism.





















Third improvement once more based on tunnels



Third improvement once more based on tunnels



Third improvement once more based on tunnels





















Last improvement: taking a look at the grid



Last improvement: taking a look at the grid


Last improvement: taking a look at the grid



Last improvement: taking a look at the grid



We have introduced the main ideas but these are not the actual routes we use. Unfortunately, due to the lack of time, we cannot explain them in more details.

Our contributions

First deterministic approach algorithm for a fully asynchronous setting whose cost is polynomial in the initial distance and the length of the labels.

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Open question

Impact of the GPS on the cost ?